NAME $\qquad$

121/1
MATHEMATICS ALT A
PAPER 1
JULY/AUGUST, 2015
TIME: $\mathbf{2}^{1 ⁄ 2} 2$ HOURS

## CENTRAL KENYA NATIONAL SCHOOLS JOINT MOCK - 2015

## Kenya Certificate of Secondary Education

MATHEMATICS ALT A
PAPER 1
TIME: $\mathbf{2}^{1 ⁄ 2} 2$ HOURS

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## FOR EXAMINER'S USE ONLY:

## SECTION I

| $\mathbf{1}$ | $\mathbf{2}$ | 3 | $\mathbf{4}$ | $\mathbf{5}$ | 6 | 7 | $\mathbf{8}$ | 9 | $\mathbf{1 0}$ | $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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SECTION II

| $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | TOTAL |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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## Mathematics Paper 1 <br> SECTION I: (50 MARKS)

Turnover

Answer all the questions in this section in the spaces provided.

1. Evaluate: $\frac{44--28}{12 \times-2}-\frac{8^{2} \times-12-24}{96 \div-12 \times 9}$
2. A basket ball team play 10 matches in a tournament. The following are scores in each match.
$9,15,17,16,7,20,21,15,10,12$
Determine:
(a) the mode.
(b) the median. later sold the cell phone for Ksh. 3120 making a profit of $30 \%$ calculate the amount of money the wholesaler had paid for the cell phone.
3. Given that $\operatorname{Cos}\left(\chi+20^{\circ}\right)=0.7660$, find $\chi$ for $0^{\circ} \leq \chi \leq 360^{\circ}$.
4. (a) Express 1050 in terms of its prime factors.
(b) Determine the smallest positive number such that 1050 p is a perfect square.
5. The exterior angle of a regular polygon is $(\chi-50)^{\circ}$ and the interior angle is $(2 \chi+20)^{\circ}$. Find the number of sides of the polygon.
6. A line $P$ passes through the point $(-2,5)$ and has a gradient of $\frac{-3}{4}$. Another line $Q$ is perpendicular to P and meets it at a point where $y=\frac{1}{2}$ find equation of Q . (4 marks)
7. Simplify the expression completely.
$\frac{(\chi+2 y)(\chi-2 y)-(\chi-2 y)^{2}}{\chi^{2}-4 y^{2}}$
8. The mass of two similar solid are 324 g and 768 g . Find
(a) height of the smaller solid if the height of the bigger solid is 20 cm . (2 marks)
(b) the surface area of the smaller solid if the surface area of the bigger solid is $40 \mathrm{~cm}^{2}$.
9. A cylindrical pipe 5 metres long has an internal diameter 28 millimetres and an external diameter of 42 millimetres. The density of the material that makes the pipe is
$1.45 \mathrm{~g} / \mathrm{cm}^{3}$. Calculate the mass of the pipe in kilograms. $\left(\right.$ Take $\left.\pi=\frac{22}{7}\right) . \quad$ ( 4 marks)
10. Simplify: $\frac{32^{\frac{-1}{5}} \times 8100^{\frac{3}{4}}}{8^{\frac{-1}{2}} \times 5^{\frac{1}{2}} \times 4^{o} \times 4^{\frac{1}{4}}}$.

Mathematics Paper 1
12. In the figure below PQRS is a rhombus, $\angle \mathrm{SQR}=55^{\circ}, \angle \mathrm{QST}$ is a right angle and TPQ is a straight line.


Find the size of the angle STQ.
(3 marks)
13. The mass of a mixture $A$ of beans and maize is 72 kg . The ratio of beans to maize is 3: 5 respectively. Find the mass of maize in the mixture.
(3 marks)
14. A square toilet is covered by a number of whole rectangular tiles of sides 60 cm by 48 cm . Calculate the least possible area of the room in square metres.
(3 marks)

Mathematics Paper 1
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Cekenas Joint Mock
15. Form the inequalities represented by region R.

16. A point C is on a line PQ where $\mathrm{PQ}=9 \mathrm{~cm}$. C divides PQ such that $P C=\frac{4}{7} P Q$. By construction locate C .

Answer any FIVE questions from this section in the spaces provided.
17. A construction company requires to transport 288 tonnes of stones to sites P and Q . The company pays 48,000 to transport 48 tonnes of stones for every 28 km . Joyce transported 96 tonnes to site $\mathrm{P}, 49 \mathrm{~km}$ away.
(a) Find how much she was paid.
(3 marks)
(b) Joyce spends Ksh. 6000 to transport every 8 tonnes of stones to site P. Calculate her total profit.
(c) Kimani transported the remaining stones to site Q, 84 km away. If he made $44 \%$ profit, find his transport cost.
18. (a) A square carpet is laid on the floor of a room so that one of its sides is against a side of a room. If leaves strips of uncovered floor 1 m wide along the two opposite sides and 2 m wide along the remaining side. If the area of the room is $64 \mathrm{~m}^{2}$, find the dimensions of the carpet.
(b) Solve the equation: $\quad \frac{y+3}{24}=\frac{1}{y-2}$.
19. A trader bought 8 cows and 12 goats for a total of Ksh.294,000. If he had bought 1 more cows and 3 more goats he would have spend Ksh.337,500.
(a) Form two equations to represent the above information.
(2 marks)
(b) Use matrix method to determine the cost of a cow and that of a goat. (4 marks)
(d) The trader sold the animals he had bought making a profit of $40 \%$ per low and $45 \%$ per goat.
(i) Calculate the total amount of money he received.
(2 marks)
(ii) Determine his profit in Kenya shillings.
20. A truck left town $X$ at 11.45 am and travelled towards town $Y$ at an average speed of $60 \mathrm{~km} / \mathrm{hr}$. A car left town X at 2.15 pm on the same day and travelled along the same road at an average speed of $100 \mathrm{~km} / \mathrm{hr}$. The distance between the two towns is 500 km .
(a) Calculate the time of the day when the car overtook the truck.
(4 marks)
(b) The distance from Y when the car overtook the truck.
(c) After overtaking the bus, both vehicles continued towards Y at their original speeds. Find how long the car had to wait at town Y before the truck arrived.
21. The displacement $S$ metres of a moving particle after $t$ seconds is given by

$$
S=2 t^{3}-5 t^{2}+4 t+2
$$

Determine
(a) the velocity of the particle when $t=2$.
(b) the value(s) of $t$ when the particle is momentarily at rest.
(c) the displacement when the particle is momentarily at rest.
(d) the acceleration of the particle when $t=5$.
22. In the figure below, $\underset{\sim}{\mathrm{OA}}=\underset{\sim}{\mathrm{a}}, \mathrm{OB}=\underset{\sim}{\mathrm{B}}$ and $\mathrm{O} \underset{\sim}{C}=3 \mathrm{O} \underset{\sim}{\mathrm{B}}$.


A
(a) Express in terms of $\underset{\sim}{a}$ and $\underset{\sim}{b}$.
(i) $\quad \underset{\sim}{\mathrm{AB}}$
(ii) $\mathrm{A}_{\sim}^{\mathrm{A}}$
(b) Given that $\underset{\sim}{\mathrm{AM}}=\frac{3}{4} \underset{\sim}{\mathrm{AB}}$ and $\underset{\sim}{\mathrm{AN}}=\frac{1}{2} \underset{\sim}{\mathrm{AC}}$, express $\underset{\sim}{\mathrm{OM}}$ and $\underset{\sim}{\mathrm{ON}}$ in terms of $\underset{\sim}{a}$ and $\underset{\sim}{b}$.
(c) Hence show that $\mathrm{O}, \mathrm{M}$ and N are collinear.
(a) Draw triangle ABC and $\mathrm{A}^{1} \mathrm{~B}^{1} \mathrm{C}^{1}$ on the same grid.
(b) Describe fully a single transformation that maps triangle ABC onto triangle $\mathrm{A}^{1} \mathrm{~B}^{1} \mathrm{C}^{1}$.
(c) On the same grid draw triangle $\mathrm{A}^{11} \mathrm{~B}^{11} \mathrm{C}^{11}$ the image of triangle ABC under a reflection in line $\mathrm{Y}=-\chi$.
(d) Draw $\Delta \mathrm{A}^{111} \mathrm{~B}^{111} \mathrm{C}^{111}$ such that it can be mapped onto triangle ABC by a negative quarter turn about the origin.
(e) Find the matrix of transformation that maps triangle ABC onto triangle $\mathrm{A}^{111} \mathrm{~B}^{111} \mathrm{C}^{111}$.

24. Arc of a circle of radius 40 cm subtends an angle of $126^{\circ}$ at the centre of the circle. (a) Calculate:
(i) the length of the arc.
(ii) the area of the sector.
(b) The sector is folded to form a cone. Calculate:
(i) the radius of the base of the cone.
(ii) the height of the cone.
(iii) the capacity of the cone in litres.

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MATHEMATICS ALT A
PAPER 2
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Kenya Certificate of Secondary Education
MATHEMATICS ALT A
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| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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SECTION II

| $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ | $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | TOTAL |
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Answer all the questions in this section in the spaces provided.

1. Simplify: $\frac{2 \frac{1}{4}-1 \frac{2}{3}}{\frac{1}{6}-\left(\frac{-1}{3}\right)^{2}}-\frac{5}{8}$ of 3 .
(4 marks)
2. (a) Expand $(2+\chi)^{4}$.
(b) Use the expansion in (a) above to. Find the value (2.01) $)^{4}$ to $4 \mathrm{~d} . \mathrm{p}$.
3. Solve for $y$ in the equation.
$\log _{10}(3 y+2)-1=\log _{10}(y-4)$.

## Mathematics Paper 2

4. Make P the subject of the formula.

$$
\mathrm{E}+\chi=\chi+\sqrt{\frac{P-3 u}{y-3 \chi P}} .
$$

5. Points $P, Q$ and $R$ are points on the circumference of a circle. If $P Q=P R=13 \mathrm{~cm}$ and $\mathrm{QR}=10 \mathrm{~cm}$, what is the radius of the circle.
(3 marks)
6. Find the radius and the centre of the circle whose equation is:

$$
3 \chi^{2}+3 y^{2}-6 \chi+12 y+3=0
$$

7. Find C that divide AB externally in the ratio 5: 2, given that A $(3,-6,9)$ and $B(-15,3,12)$.
8. A two digit number is formed from the first four prime numbers.
(a) Draw the table to show the possible out comes.
(b) Calculate the probability that a number chosen from the two digits is even number.
9. A dam containing $4158 \mathrm{~m}^{3}$ of water is to be drained. A pump is connected to a pipe of radius 3.5 cm and machine operate for 8 hours per day. Water flows through the pipe at the rate of 1.5 m per second. Find the number of days it takes to drain the dam.
(4 marks)
10. The population of two town Kana and Jane for three years were as follows:

Kana 40,000, 48000, 56000
Jane 40,000, 48000, 57600
Calculate the difference in population of the two after six years.

Mathematics Paper 2
11. The gradient of a curve at any point given by $2 \chi-1$. Given that the curve passes through point $(1,5)$. Find the equation of the curve.
12. Simplify: $\frac{3}{\sqrt{7}-\sqrt{2}}-\frac{2}{\sqrt{7}+\sqrt{2}}$.
13. Given that $\mathrm{AB}=6 \mathrm{~cm}$ construct locus of P such that angle $\angle \mathrm{APB}=90$.
14. A car valued at Ksh.500,000 in January 2008. Each year, it value depreciates at $12 \%$ p.a. Find after how long would the value depreciate to Ksh.250,000.

## Mathematics Paper 2

Cekenas Joint Mock
15. In below figure $\mathrm{PT}=4 \mathrm{~cm}$ and $\mathrm{TQ}=5 \mathrm{~cm}$ and $\mathrm{TS}=2.5 \mathrm{~cm}$ find TR by calculation.

16. Given that $2 \leq \mathrm{A} \leq 4$ and $0.1 \leq \mathrm{B} \leq 0.2$. Find the minimum value of $\frac{A B}{A-B}$.

## SECTION B: (50 MARKS)

Answer any FIVE questions from this section in the spaces provided.
17. Two towns A and B lie on the same parallel of latitudes $60^{\circ} \mathrm{N}$. If the longitudes of A and B are $42^{\circ} \mathrm{W}$ and $29^{\circ} \mathrm{E}$ respectively.
(a) Find the distance between A and B in nautical miles along the parallel of latitude.
(b) Find the local time at A if at B is 1.00 pm .
(c) Find the distance between A and B in $\mathrm{km} .\left(\right.$ Take $\pi=\frac{22}{7}$ and $\left.R=6370 \mathrm{~km}\right)$. (2 marks)
(d) If C is another town due South of A and 10010 km away from A, Find the co-ordinate of C .

Mathematics Paper 2
18. In the figure below AOC is a diameter of the circle centre $\mathrm{O} . \mathrm{AB}=\mathrm{BC}$ and $\angle \mathrm{ACD}=35^{\circ}, \mathrm{EBF}$ is a tangent to the circle at B . G is a point on minor arc CD .


Calculate the size of the following angles giving reasons in each case.
(a) $\angle B C D$.
(b) Obtuse angle BOD.
(c) $\angle \mathrm{BAD}$.
(d) $\angle$ CGD.
(e) $\angle \mathrm{AEB}$.
(2 marks)

Mathematics Paper 2
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Cekenas Joint Mock
19. (a) Complete the table below for the function $\mathrm{y}=3 \chi^{2}-2 \chi-1$ for $-3 \leq \chi \leq 4$.

| $\chi$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{y}=3 \chi^{2}-2 \chi-1$ |  | 15 |  |  |  | 7 |  |  | (2 marks)

(b) Draw the graph of $y=3 \chi^{2}-2 \chi-1$.


Mathematics Paper 2
(c) Draw the line $y=3 \chi+1$ on the same axis hence find the values of $\chi$ for which $\mathrm{y}=3 \chi+1$ and y $3 \chi^{2}-2 \chi-1$ are equal.
(d) Write down the simplified quadratic equation whose roots are the solutions of the simultaneous equation in (c) above.
20. The diagram below shows a right pyramid VPQRS with V as the vertex and a rectangular base $\mathrm{PQRS} . \mathrm{PQ}=3 \mathrm{~cm}, \mathrm{QR}=4 \mathrm{~cm}$. The height of the pyramid is 6 cm . $P M=M Q$ and $O Q=N R$.

(a) Calculate.
(i) the length PV.
(ii) the angle between face VPQ and the base.

## (b) (i) the slant height VM and VN.

(ii) What is the surface area of the pyramid?
21. On the same axes, draw this graph of $y=2 \operatorname{Sin} \chi$ and $y=3 \operatorname{Sin}\left(\chi+30^{\circ}\right)$ for the domain $-360^{\circ} \leq \chi \leq 360^{\circ}$.
(a) the period of each of the functions.
(b) the amplitude of each of the functions.
(c) the solution to $2 \operatorname{Sin} \chi=3 \operatorname{Sin}\left(\chi+30^{\circ}\right)$.
(d) the transformation that maps the graph of $\mathrm{y}=2 \operatorname{Sin} \chi$ onto the graph of $y=3 \operatorname{Sin}\left(\chi+30^{\circ}\right)$.

Mathematics Paper 2
22. The diagram below shows a histogram marks obtained in a certain test.

(a) Develop a frequency distribution table for the data if the first class 5-9 has a frequency of 8 .
(c) Calculate interquatile range.
23. The cost C , of producing n items varies partly as n and partly as the inverse of n . To produce two items it cost 50Sh and to produce six items it costs 70Sh. Find
(a) the constants of proportionality and hence write the equation connecting C and n .
(b) the cost of producing 12 items.
(c) the number of items produced at a cost of 106 Sh . type A cost $S h .40$ per 100 ml tin and type B cost $S h .60$ per 100 ml tin. He decided to buy at least 30 tins altogether of type A and B with Sh. 1500 available. He decides that at least one third of the tins should be of type B. He buys $\chi$ tins of type A and y tins of type B.
(a) Write down three inequalities, which represent the above information. (3 marks)
(b) On a graph paper, draw a graph to show the three inequalities (a) above. (3 marks)

(c) Determine how many tins of each type that he should buy to maximize his profit if he makes a profit of Sh .10 of each type A and a profit of Sh .20 on each type B tin.
(d) Calculate maximum possible profit.

